



## Analytical Study of Biomass Cloud Particles considering the Lewis number effect

Milad Shokouhmand<sup>\*,§</sup>, Payam Asadollahzadeh<sup>\*\*</sup> and Mehdi Bidabadi<sup>\*\*\*</sup>

<sup>\*</sup> Ms.c Graduate of Aerospace Engineering, IUST, School of Mechanical Eng.

<sup>\*\*</sup> Ms.c Graduate of Mechanical Engineering, IUST, School of Mechanical Eng

<sup>\*\*\*</sup> Associated professor of IUST, School of Mechanical Eng

(<sup>§</sup>Correspondent author's E-mail: milad.shokouhmand@gmail.com)

**ABSTRACT:** In this paper, the effect of Lewis number on the structure of one-dimensional flame of biomass combustion is analyzed. This effect can be observed by considering the non-unity Lewis number in the governing equations. the value of the characteristic Zeldovich number is too large and the equivalence ratio is larger than unity  $\phi_u \geq 1$  The flame structure consists of three different zones which are, a preheat vaporization zone a reaction zone that consists of gas and Char combustion and a convection zone. The obtained results from the present model declare that the temperature and burning velocity profiles are extremely affected by the various Lewis numbers.

**Keywords:** Biomass particle, Lewis number, Burning rate.

## INTRODUCTION

Biomass is a clean and renewable source of energy and currently represents nearly 14-15% energy consumption. In fact, the necessity of biomass varies significantly across regions of the world. Biomass is becoming a more and usable fuel in the developed countries and because of the diversity of this general source of energy, so many scientists all around the world focus their studies on the different aspects of mathematically, numerically and experimentally modeling of biomass and organic fuels (Chen et al., 1998; William et al., 2001; Backreedy et al., 2002). The selection and design of any biomass combustion system is mainly depended on the characteristics of the fuel (Chopra and Jain, 2007). There are wide ranges of biomass fuels such as wood, short-rotation woody crops and herbaceous species which are studied for at least 20 years. Also the study of biomass/coal co-firing because of the greenhouse emission is the goal of combustion scientist (Senneca, 2007). SO<sub>2</sub> and NO<sub>x</sub> are alternatively biomass pollutant which can be pyrolysed or gasified producing a liquid fuel or a gas-like fuel such as carbon monoxide. Pyrolysis actually is the thermal destruction processes of organic materials and it is pursued by heating in the absence or shortage of oxygen. Fuel moisture content, fuel volatile content, and in the case of combustion on the fuel bed, air flow rate through the bed are the critical factors affecting the ignition velocity. Saastamoinen et al. (2001) experimentally and theoretically studied the ignition wave propagation against the air flow in different packed beds of wood fuels and considered the extra factors such as air temperature,



bulk density of the fuel bed and particle size. Lu et al. (2009-In Press) experimentally and theoretically indicated the influence of particle shape and size on the biomass particle dynamics, including drying, heating and reaction rate. Wornat et al. (1996) experimentally studied on the two different type of single particle of biomass char and achieved the burning rates and compare them to the high-volatile bituminous coals. C. Ryu et al. (2006) in their study experimentally investigates the combustion of four biomass materials having different fuel properties in a fixed bed under fuel-rich conditions. Also Y.B. Yang et al. (2004) experimentally and analytically studied on the effect of primary airflow rate and fuel moisture of biomass solid wasted fuel and declare that Primary air has an important effect on the sub-processes combustion: moisture evaporation, devolatilisation and char burning. In addition, they claimed that increasing primary airflow initially increases each of the process rates but causes a decrease in the rates beyond the critical airflow rate. Cetin et al. (2005) experimentally studied on the on the influence of Pressure of combustion area on the char structure and gasification kinetics and in their study some results are achieved by the variation of combustion pressure and they analysis the activation energy and frequency factor in Arrhenius equation. In this article the variation effect of Lewis number in a combustion process of biomass fuel particle considering the Char and Tar formation including the heat of vaporization and devolatilization of fuel particles is modeled. The governing equations are solved mathematically and the achieved results are plotted numerically.

### Physical Modelling

In this process biomass, cloud particles ignited right after the vaporization of their moisture and Char material is generated at the same time and react with oxidizer. During the combustion of biomass particles like wood five volatied material such as CO , CO2 , H2 , H2O and one light hydrocarbon are produced. It is assumed that the rate of gas burning velocity and porous material burning velocities has the same value. the rate of flame propagation is depended on the 1-the rate of the heat exchanged from the flame, 2- thermodynamical equilibrium of gas phase and solid, in the burned zone

### Mathematical Modelling

In the present work, the number and radius of the particles are considered to be known as the primary data and it should also be noticed that all external forces such as gravitational field on earth are neglected in this study. the structure of premixed flames propagation in combustible system, containing uniformly distributed gaseous fuel, char, tar and oxidizing gas mixture, is analyzed.

### Governing Equations

Mass Conservation Equation:

$$\rho V = cte \tag{1}$$

Energy conservation equation:

$$\tag{2}$$



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$$\rho v C \left( \frac{dT}{dx} \right) = \lambda_u \left( \frac{d^2 T}{dx^2} \right) + w_F \left( \frac{\rho_u}{\rho} \right) Q - w_v \left( \frac{\rho_u}{\rho} \right) Q_v$$

$$+ w_c \left( \frac{\rho_c}{\rho} \right) Q_c + w_T \left( \frac{\rho_T}{\rho} \right) Q_T - w_{de} \left( \frac{\rho_u}{\rho} \right) Q_{de}$$

Where  $\rho$ ,  $v$ ,  $w_F$ ,  $w_c$ ,  $w_T$  and  $w_v$  are the density, the flow velocity, the reaction rate, the reaction rate of char, the reaction rate of tar and the rate of devolatilization respectively and also  $Y_F$  and  $Y_c$  are the mass fraction of the fuel and the mass fraction of char, respectively.  $\lambda$  is the heat conduction coefficient of both particles and gaseous fuel,  $Q$  is the heat release per unit mass of the particles fuel burned in the reaction,  $Q_v$  is the heat associated with vaporizing unit mass of fuel and  $C$  is the heat capacity of Gaseous and fuel particles combination.

Gaseous fuel conservation equation:

$$\rho v \left( \frac{dY_F}{dx} \right) = \rho_u D_u \left( \frac{d^2 Y_F}{dx^2} \right) - w_F \left( \frac{\rho_u}{\rho} \right)$$

$$+ w_v \left( \frac{\rho_u}{\rho} \right) + w_{de} \left( \frac{\rho_u}{\rho} \right) - w_T \left( \frac{\rho_T}{\rho} \right)$$
(3)

Where  $Y$  is the mass fraction of particles and  $D$  is the mass diffusion coefficient Particle mass fraction conservation equation:

$$\rho_s V \left( \frac{dY_s}{dx} \right) = -w_v \left( \frac{\rho_u}{\rho} \right) - w_{de} \left( \frac{\rho_u}{\rho} \right)$$

$$\rho V \left( \frac{dY_c}{dx} \right) = w'_c \left( \frac{\rho_c}{\rho} \right)$$
(4)

The heat capacity ( $C$ ) is a combination of heat capacity of particles ( $C_s$ ) and gas ( $C_p$ ) and it can be evaluated from this expression:

$$C = C_p + \frac{4\pi(r^3 C_s \rho_s n_s)}{3\rho}$$
(6)

Where  $r$  is the radius of particles and  $w_v$  can be described by:

$$w_v = 4\pi A n_s r^2 (T - T_u)^n$$
(7)

Where  $A$ , the Characteristic parameter of vaporization is rate of fuel particles and  $n$  is presumed to be constant.

**Non-dimensional parameters:**



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$$m = \frac{\rho v}{\rho_u v_u}, \theta = \frac{T - T_u}{T_f - T_u}, y_s = \frac{Y_s}{Y_{FC}} \quad (5)$$

$$z = \frac{\rho_u v_u C}{\lambda_u} x, y_F = \frac{Y_F}{Y_{FC}}, y_C = \frac{Y_C}{Y_{FC}}$$

Solution: By using the differential equations and asymptotical methods for different combustion zones the equations and non-dimensional equations is solved. The reaction rate is calculated by Arrhenius equ.

Also some parameters such as  $\omega_f, \omega_{de}, \omega_c, \gamma, q$  are defined as:

$$\omega_f = \frac{\lambda_u \times w_f}{(\rho_u v_u)^2 \times C \times Y_{FC}}$$

$$\omega_c = \frac{\lambda_u \times w_c}{(\rho_u v_u)^2 \times C \times Y_{FC}}$$

$$\omega_{de} = \frac{\lambda_u \times w_{de} \times Y_{FC}}{(\rho_u v_u)^2 \times C^3 \times (T_f - T_u)^2}$$

$$\omega_r = \frac{\lambda_u \times w_r}{(\rho_u v_u)^2 \times C \times Y_{FC}}$$

$$\gamma = \frac{4.836 A n_u^{1/3} \lambda_u (T_f - T_u)^n}{v_u^2 \rho_u^{1/3} C Y_{FC}^{1/3} \rho_s^{2/3}}$$

$$\gamma' = \frac{4.836 A' n_u^{1/3} \lambda_u (T_f - T_u)^n}{v_u^2 \rho_u^{1/3} C Y_{FC}^{1/3} \rho_s^{2/3}}$$

$$q = \frac{Q_u}{Q}$$

The parameters  $\gamma, \gamma'$  are presumed to be  $O(1)$ , and the dimensionless form of the boundary conditions for these equations are:

$$\theta = \theta_b = (T_b - T_u) / (T_f - T_u)$$

$$y_F = \text{finite} \quad y_C = \text{finite} \quad \rightarrow z = \infty$$

$$\theta = 0 \quad y_F = 0 \quad y_S = \alpha \quad y_C = 0 \quad \rightarrow z = -\infty$$

Where  $v_u$  characteristic burning velocity of the flame propagation neglecting the particles is heat of vaporization and  $\alpha$  is defined by  $\alpha = Y_{FU} / Y_{FC}$ . It is assumed that the quantity of  $q$  is negligible which means that the heat released due of reaction is more than the heat absorbed due to vaporization of the particles. In this situation instead of  $\theta$ , the new parameter ( $\theta^0$ ) can be described where  $m = 1$ .

### Burning Velocity Correlation

Using equations (21) and (23), the burning velocity of fuel particles can be obtained as below:



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$$v_u^2 = \frac{2(L_e + b)\lambda_u \varepsilon^2 (v_F k_F + v_C k_C + v_T k_T)}{\rho_u C} \quad (6)$$

And if two parameters  $T_f$  and  $b$  are presumed to be known, value  $v_u$  can be calculated. For high value of  $T_f$ , it is reasonable to assume that  $y_{Ff} = 0$  which is resulted to  $b = 0$ . Flame temperature ( $T_f$ ) is evaluated by the jump conditions of preheat-vaporization zone and convection zone. The jump condition is written as:

$$\left[ \frac{dy_F}{dz} \right]_{0^-} + \left[ \frac{d\theta^0}{dz} \right]_{0^-} + \left[ \frac{dy_C}{dz} \right]_{0^-} = \left[ \frac{dy_F}{dz} \right]_{0^+} + \left[ \frac{d\theta^0}{dz} \right]_{0^+} + \left[ \frac{dy_C}{dz} \right]_{0^+} \quad (7)$$

### RESULTS

In the combustion of the wood particles, it is presumed that the fuel particles vaporize first to yield the methane structure. The chemical kinetic rate parameters are  $E = 25000 \text{ Cal/mole}$  and  $B = 5.16 \times 10^6 \text{ mol}^{-1} \text{ s}^{-1}$ . Also the kinetic of vaporization of fuel particles are prescribed by these assumptions:

$$A = 3.4 \times 10^{-4} (g)_F / [(cm^2)_s ks], \quad n = 1.33.$$

The constant parameters are presumed are

$$\lambda_u = 3 \times 10^{-4} (cal/cm.s.k), \rho_u = 1.13 \times 10^{-3} (g/cm^3), \rho_s = 0.72 \times 10^{-3} (g/cm^3), T_u = 300K, q = 0.01$$

It is shown that for  $\phi_u \geq 1$  the equivalence ratio based on the fuel available in the fuel particles ( $\phi_u$ ) are formulated by  $\phi_u = 17.18 Y_{Fu} / (1 - Y_{Fu})$ . Also the effective equivalence ratio in the reaction zone ( $\phi_g$ ) is calculated by  $\phi_g = 17.18 Y_{FC} / (1 - Y_{FC})$ .

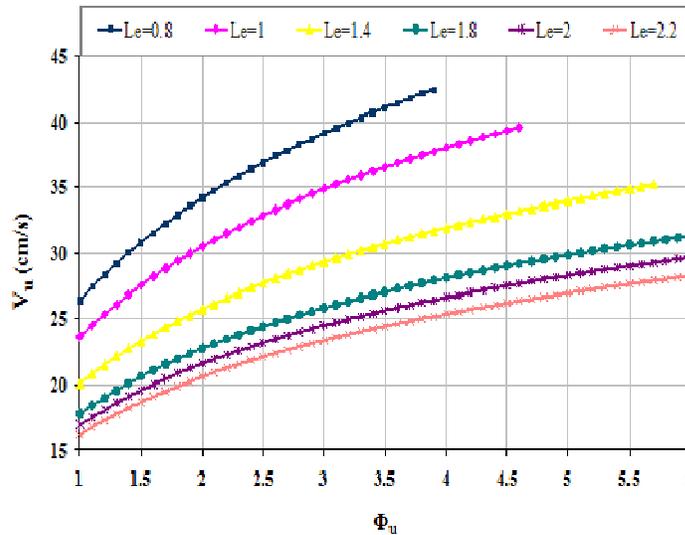


Fig. 1. The variation of burning velocity, neglecting the heat of vaporization, as a function of equivalence ratio for different Lewis numbers at  $R = 20\mu m$

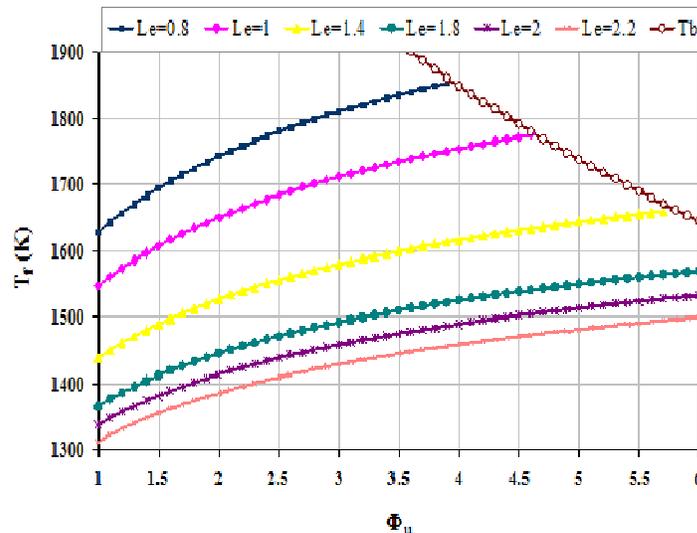


Fig. 2. The variation of flame temperature as a function of equivalence ratio for different Lewis numbers at  $R = 20\mu m$

### CONCLUSIONS

This article analytically investigates the combustion properties of biomass particles. The initial combustion properties of the biomass particles for instance flame adiabatic temperature and heat capacity of the fuel and air mixture as a function of equivalence ratio are calculated via the standard computer program. And also in this paper the variation of burning velocity and the flame temperature via the particles size and thermal properties is shown and illustrated because of the extremely dependence to those parameters. It is observed that Lewis number is a determining factor on the combustion properties of biomass particles and the rise in the Lewis number coincides with the reduction in the flame temperature and burning velocity. Similarly, it is declared that the lower flame temperature and burning velocity are gained for larger size of the particles. Consequently, the variation of  $\phi_g$  as a function of  $\phi_u$  elucidates that the quantity of  $\phi_g$  is less than unity and it does not tend to the stoichiometric condition, while  $\phi_u$  is larger than unity. That's why the temperature and burning velocity profiles increase due to increasing the  $\phi_u$ . A characteristic value temperature  $T_v$  could be chosen, such that for particle temperature less than  $T_v$ , vaporization effects can be ignored and where the gas temperature is larger than  $T_v$ , the temperature of the particles is presumed to be constant and has a same value with gas. To describing the condition of steady states flame propagation, non adiabatic consideration concepts are employed. The increase in  $T_v$  associated with the decrease in the burning velocity which mathematically and physically express that at higher  $T_v$ , the higher temperature is needed for



starting the vaporization process and the theory declare that since the  $T_v$  increase, the mass fraction of the biomass dust particles move towards the reaction zone. It found that excess oxygen would leak from the reaction zone into the convection zone if  $\phi_u \geq 1$  and  $\phi_g \leq 1$ . Similarly it is declared that the lower flame temperature and burning velocity are gained for larger size of the particles. Concluding the high temperature vaporization of the fuel particles in convection zone is continued and presumed one-step reaction between vaporized particles and oxygen is expected to be occurred. Gaseous fuel particle mass fraction at both preheats and vaporization zone decrease and increase respectively when the Lewis number increases. Burning separately with a diffusion flame surrounding the particles in convection zone the variation of  $\phi_g$  as a function of  $\phi_u$  elucidates that the quantity of  $\phi_g$  is less than unity and it doesn't tend to the stoichiometric condition, while  $\phi_u$  is larger than unity. And it declare that the temperature and burning velocity profiles increase due to increasing the  $\phi_u$ . even for the large values of  $\beta_2$  cloud particles combustion occurred in the reaction zone. The model declare that the increase in  $T_v$  reaches to the level which the amount of the gaseous fuel mass fraction and the onset of the vaporization and highest level of the plot move forward the reaction zone and it express the major influence of Lewis number which lead to the flame approaches towards the reaction zone. In the particle cloud combustion including the vaporization of particles, which is happened in the convective, zone the rate of oxidation of  $H_2$  and  $CO$  to  $H_2O$  and  $CO_2$  can be ignored.

### NOMENCLATURE

$A$  : Parameter characterizing rate of vaporization of fuel particles

$Y_{FC}$  : Parameter characterizing rate of vaporization of fuel particles

$B$  : Frequency factor characterizing rate of gas Phase oxidation of the gaseous fuel

$C$  : Heat capacity of mixture

$C_F$  : Molar concentration of fuel

$C_p$  : Heat capacity of the gas

$C_s$  : Heat capacity of a fuel particle

$D$  : Diffusion coefficient

$E$  : Activation energy characterizing the gas-Phase reaction

$k$  : Rate constant of the gas-phase reaction

$Le$  : Lewis Number

$n$  : Temperature exponent characterizing rate of vaporization of fuel particles

$n_s$  : Local number density of particles (number of particles per unit volume)

$n_u$  : Number density of particles in ambient reactant stream (number of particles per unit volume)

$Q$  : Heat release per unit mass of gaseous fuel consumed

$Q_v$  : Heat associated with vaporizing unit mass of fuel

$Q_c$  : Heat associated with charring unit mass of fuel

$Q_T$  : Heat associated with Tarring unit mass of fuel



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- $R$  : Gas constant  
 $r$  : Radius of fuel particle  
 $T$  : Temperature  
 $t$  : Defined in Eq. 22  
 $V$  : Velocity  
 $V_u$  : Burning velocity calculated neglecting heat of vaporization of fuel particles  
 $V_v$  : Burning velocity calculated including heat of vaporization of fuel particle  
 $W_F$  : Molecular weight of gaseous fuel  
 $w_v$  : Rate of vaporization of fuel particles  
 $w_{de}$  : Rate of vaporization of fuel particles  
 $w_c$  : Rate of char of fuel particles  
 $w_T$  : Rate of Tar of fuel particles  
 $w_F$  : Reaction rate characterizing consumption of gaseous fuel  
 $Y$  : Mass fraction  
 $y$  : Gaseous fuel available in the particles in the Ambient reactant stream Defined in Eq. 22  
 $Y_{Fu}$  : Gaseous fuel available in the particles in the Ambient reactant stream  
 $z_e$  : Zeldovich number,

### Greek Symbols

$$\alpha = \frac{Y_{Fu}}{Y_{FC}}$$

$\gamma$  : Defined in Eq

$\gamma'$  : Defined in Eq.

$$\varepsilon = \frac{1}{Z_e} \text{ Expansion parameter}$$

$\eta$  : Independent variable defined in Eq. 19

$\theta$  : Defined in Eq. 11

$\theta^0$  : Value of  $\theta$  calculated neglecting heat of Vaporization of particles

$\Lambda$  : Defined in Eq. 21

$\lambda$  : Thermal conductivity

$\rho$  : Density of the reactant mixture

$\rho_s$  : Density of a fuel particle

$\nu$  : Stoichiometric coefficient

$\phi_u$  : Equivalence ratio based on fuel available in The particles in the ambient reactant stream

$\phi_s$  : Effective equivalence ratio in the reaction zone

$\omega$  : Defined in Eq. 10

### Subscripts

$b$  : Adiabatic conditions after completion of Chemical reactions

$F$  : Gaseous fuel

$f$  : Conditions at the reaction zone



## REFERENCES

- Backreedy, R.I., J.M. Jones, M. Pourkashanian and A. Williams,[2002] “Modelling the reaction of oxygen with coal and biomass chars,” Proceedings of the Combustion Institute, 29, 415–422
- Biagini, E., Simone, M., Tognotti, L.,[2009] “Characterization of high heating rate chars of biomass fuels,” Proceedings of the Combustion Institute
- Bidabadi, M., and A. Rahbari,[2009] “Modeling combustion of lycopodium particles by considering the temperature difference between the gas and the particles,” Combustion Explosion and Shockwaves, 45, 49-57
- Bidabadi, M., and A. Rahbari, [2009] “Novel analytical model for predicting the combustion characteristics of premixed flame propagation in lycopodium dust particles,” Journal of Mechanical Science and Technology, 23, 1911-1923
- Bidabadi, M., A.Haghiri, and A.Rahbari, [2010] “The effect of Lewis and Damköhler numbers on the flame propagation through micro-organic dust particles,” International Journal of Thermal Sciences (In Press)
- Bidabadi, M., Shokouhmand, M., Fereydooni, J., Rahbari, A.,[2009] “Propagation of the reaction front of dry biomass particles in a fixed bed.” 22nd International Colloquium on Dynamics of Explosions and Reactive Systems (ICDERS)
- Calle, S., L.Klaba, D.Thomas, L.Perrin, and O.Dufaud, [2005] “Influence of the size distribution and concentration on wood dust explosion: Experiments and reaction modelling,” Powder Technology, 157, 144 – 148
- Cetin, E., Moghtaderi, B., Gupta, R. and Wall, T.F., [2005] “Biomass gasification kinetics: influences o pressure and char structure,” Combust. Sci. and Tech., 177: 765–791, (2005
- Ritchie, G.S. [1983], Nonlinear Dynamic Characteristics of a Finite Journal Bearing, Trans. ASME, J. Lub. Tech., Vol. 1, No. 3, pp. 375-376.